

# **Exploding Dots**<sup>™</sup>

## HANDOUTS

### **Experience 3:**

## **Addition and Multiplication**

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### **Exploding Dots**

#### **Experience 3: Addition and Multiplication**

Access videos of all *Exploding Dots* lessons at: <u>http://gdaymath.com/courses/exploding-dots/</u>

#### Handout A: Addition

Here is the Exploding Dots way to add 358 and 287.

358	:	:::	#
+ 287	••	#	÷
=	ŀ	:::·	

Explosions then show that this answer is equivalent to 645.

Write down the answers to the following addition problems working left to right and not worrying about what society thinks! Then, do some explosions to translate each answer into something society understands.

148	567	377	582
+ 323	+ 271	+ 188	+ 714
=	=	=	=
310462872		87263716381	
+ 389107123		+ 18778274	824
=		=	



#### **Solutions to Handout A**

148 + 323 = 4 | 6 | 11 = 471

 $567 + 271 = 7 \mid \! 13 \mid \! 8 = 838$ 

377 + 188 = 4 | 15 | 15 = 5 | 5 | 15 = 565

582+714=12|9|6=1|2|9|6=1296

310462872 + 389107123 = 6 | 9 | 9 | 5 | 6 | 9 | 9 | 9 | 5 = 699569995

87263716381 + 18778274824 = 9 | 15 | 9 | 13 | 11 | 9 | 8 | 10 | 11 | 10 | 5= ... = 106041991205





Handouts



#### **Solutions to Handout B**

We have

 $26417 \times 4 = 8 | 24 | 16 | 4 | 28 = 10 | 4 | 16 | 4 | 28 = 1 | 0 | 4 | 16 | 4 | 28 = 1 | 0 | 5 | 6 | 4 | 28 = 105668$  $26417 \times 5 = 10 | 30 | 20 | 5 | 35 = 10 | 30 | 20 | 8 | 5 = 10 | 32 | 0 | 8 | 5 = 13 | 2 | 0 | 8 | 5 = 132085$  $26417 \times 9 = 18 | 54 | 36 | 9 | 63 = 18 | 54 | 36 | 15 | 3 = ... = 237753$ 

 $26417 \times 10 = 20 | 60 | 40 | 10 | 70 = \dots = 264170$ 

and

26417×11 = 22 | 66 | 44 | 11 | 77 = ... = 290587

 $26417 \times 12 = 24 | 72 | 48 | 12 | 84 = ... = 317004$ 

For a full discussion as to why  $26417 \times 10$  is 264170 have a look at Lesson 3.5 of <u>http://gdaymath.com/courses/exploding-dots/</u>.



### **Exploding Dots**

#### **Experience 3: Addition and Multiplication**

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#### Handout C: WILD EXPLORATIONS

Here are some "big question" investigations you might want to explore, or just think about. Have fun!

**EXPLORATION 1: THERE IS NOTHING SPECIAL ABOUT BASE TEN FOR ADDITION** 

Here is an addition problem in a  $1 \leftarrow 5$  machine. (That is, it is a problem in base five.) This is not a  $1 \leftarrow 10$  machine addition.

#### 20413 <sub>+</sub> 13244

- a) What is the  $1 \leftarrow 5$  machine answer?
- b) What number has code 20413 in a 1 ← 5 machine? What number has code 13244 in a 1 ← 5 machine? What is the sum of those two numbers and what is the code for that sum in a 1 ← 5 machine?

[Here are the answers so that you can check your clever thinking.

The sum, as a  $1 \leftarrow 5$  machine problem, is

20413+13244 = 3 | 3 | 6 | 5 | 7 = 3 | 4 | 1 | 5 | 7 = 3 | 4 | 2 | 0 | 7 = 3 | 4 | 2 | 1 | 2 = 34212

In a 1  $\leftarrow$  5 machine, 20413 is two 625's, four 25's, one 5, and three 1's, and so is the number 1358 in base ten; 13244 is the number 1074 in base ten; and 34212 is the number 2432 in base ten. We have just worked out 1358 + 1074 = 2432.]



**EXPLORATION 2: THERE IS NOTHING SPECIAL ABOUT BASE TEN FOR MULTIPLICATION** 

Let's work with a  $1 \leftarrow 3$  machine.

a) Find 111  $\times$  3 as a base three problem. Also, what are 1202  $\times$  3 and 2002  $\times$  3?

Can you explain what you notice?

Let's now work with a  $1 \leftarrow 4$  machine.

b) What is  $133 \times 4$  as a base four problem? What is  $2011 \times 4$ ? What is  $22 \times 4$ ?

Can you explain what you notice?

In general, if we are working with a  $1 \leftarrow b$  machine, can you explain why multiplying a number in base b by b returns the original number with a zero tacked on to its right?

